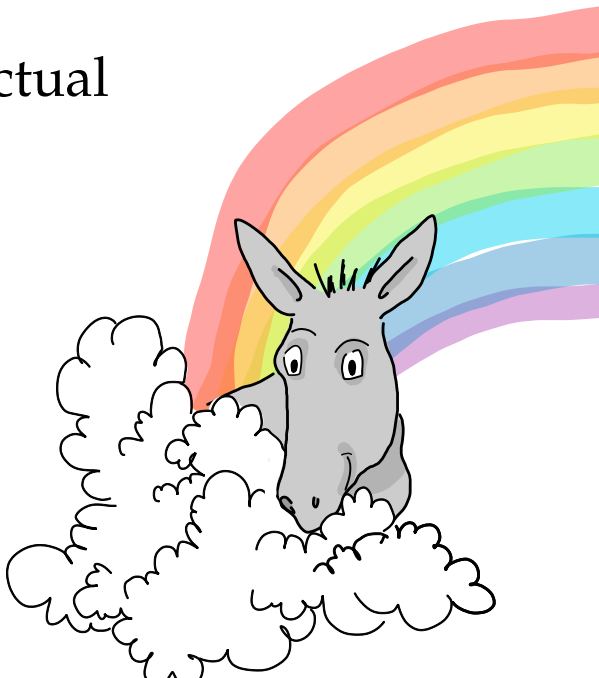


Counterfactual
Donkeys
Don't
Get High

Mike Deigan
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New Data

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Suppose Allie and Bert think Mary the potter probably didn't make anything yesterday.

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(1) *Allie:*

New Data

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- (1) *Allie*: If Mary had made a vase, she would have made it from glass.

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Case 1: Mary actually made two vases, both from glass.

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Judgements: (1) ✓ (2) ??

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Case 2:

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Case 2: Mary did not make any vases.

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Suppose Allie and Bert think Mary the potter probably didn't make anything yesterday.

- (1) *Allie*: If Mary had made a vase, she would have made it from glass. ✗

Case 2: Mary did not make any vases.

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New Data

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New Data - Summary

- (1) *Allie*: If Mary had made a vase, she would have made it from glass.
- (2) *Bert*: But she could have made a clay vase (and she wouldn't have made *that* from glass)!

Case 1: Mary made two glass vases.

Case 2: Mary did not make any vases.

	Case 1	Case 2
(1)	✓	✗
(2)	??	✓

So what?

Old Data

(3) If Balaam owned a donkey, he would beat it.

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Apparent entailments:

(4) a. If Herbert were a donkey Balaam owned, Balaam would beat Herbert.

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Apparent entailments:

- (4) a. If Herbert were a donkey Balaam owned, Balaam would beat Herbert.
- b. If Eeyore were a donkey Balaam owned, Balaam would beat Eeyore.

Old Data

(3) If Balaam owned a donkey, he would beat it.

Apparent entailments:

- (4) a. If Herbert were a donkey Balaam owned, Balaam would beat Herbert.
- b. If Eeyore were a donkey Balaam owned, Balaam would beat Eeyore.
- c. If Platero were a donkey Balaam owned, Balaam would beat Platero.

Old Data - Two Accounts

Two routes to accounting for universal entailments:

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$$\exists x[Px] \Box \rightarrow Qx \quad \Leftrightarrow \quad \forall x[Px \Box \rightarrow Qx]$$

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$$\exists x[Px] \sqsupset \rightarrow Qx \quad \Leftrightarrow \quad \forall x[Px \sqsupset \rightarrow Qx]$$

(van Rooij (2006), Walker and Romero (2015))

Thesis

We should take Route 1.

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The special ordering-based accounts predict the new data.

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High reading accounts don't.

In other words. . .

Counterfactual donkeys

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Counterfactual donkeys don't get high.

Overview

Accounting for the Old Data

Ordering Semantics + Dynamic Binding

Route 1: Special Orderings

Route 2: High Readings

Returning to the New Data

The Problem for High Readings

The Success of Special Orderings

Some Objections and Replies

Saving High Readings?

Problem for Special Orderings?

Takeaway

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Ordering Semantics + Dynamic Binding

Familiar Stalnaker-Lewis style semantics.

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Selection function:

$$(5) \quad f(A, w) = \{w' : w \in \llbracket A \rrbracket \wedge \neg \exists w'' (w'' \in \llbracket A \rrbracket \wedge w'' <_w w')\}$$

The A -worlds nearest to w , according to $<_w$.

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The A -worlds nearest to w , according to $<_w$.

$$(6) \quad \llbracket A \Box \rightarrow C \rrbracket = \{w : \forall w' (w' \in f(A, w) \supset w \in \llbracket C \rrbracket)\}$$

C is true at all the nearest A -worlds.

Ordering Semantics + Dynamic Binding

DPL with possible worlds (based on Groenendijk and Stokhof (1991) and Groenendijk, Stokhof, and Veltman (1996))

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info state s : set of possibilities

update function $[\cdot]$ from a state and sentence to a state

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$$(7) \quad \text{a.} \quad s[F(x)] = \{i : i \in s \wedge w_i \in \llbracket F(g_i(x)) \rrbracket\}$$

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info state s : set of possibilities

update function $[\cdot]$ from a state and sentence to a state

- (7)
- a. $s[F(x)] = \{i : i \in s \wedge w_i \in \llbracket F(g_i(x)) \rrbracket\}$
 - b. $s[\exists x] = \{i : \exists j \exists d (j \in s \wedge d \in \mathcal{D} \wedge w_i = w_j \wedge g_i = g_j^{x \rightarrow d})\}$

Ordering Semantics + Dynamic Binding

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j is an A -possibility for i (or $j \in /A/i$) iff $\exists k(g_k = g_i \wedge j \in \{k\}[A])$.

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Finds the nearest A -possibility, where possibilities are ordered by their worlds.

Ordering Semantics + Dynamic Binding

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Finds the nearest A -possibility, where possibilities are ordered by their worlds.

$$(9) \quad s[A \Box \rightarrow C] = \{i : i \in s \wedge \forall j(j \in f(A, i) \supset \{j\}[C] \neq \emptyset)\}$$

C is verified by all selected possibilities

Ordering Semantics + Dynamic Binding

(3) If Balaam owned a donkey, he would beat it.

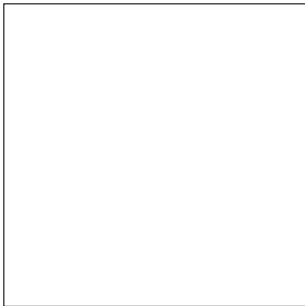
Ordering Semantics + Dynamic Binding

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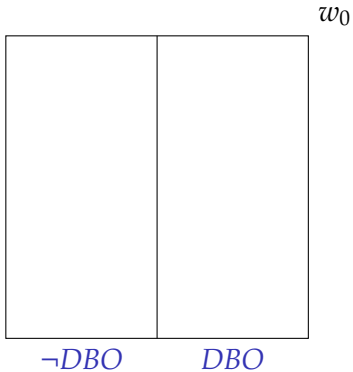
(10) $\exists x DBO(x) \Box \rightarrow BB(x)$

Dynamic Binding + Ordering Semantics

w_0

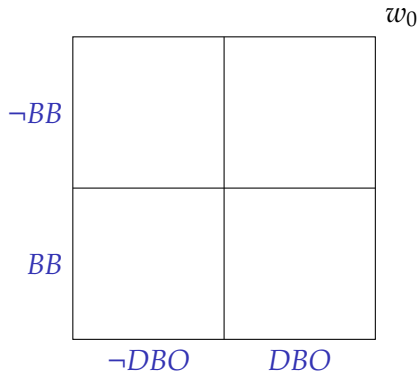


Dynamic Binding + Ordering Semantics



DBO = donkey that Balaam owns

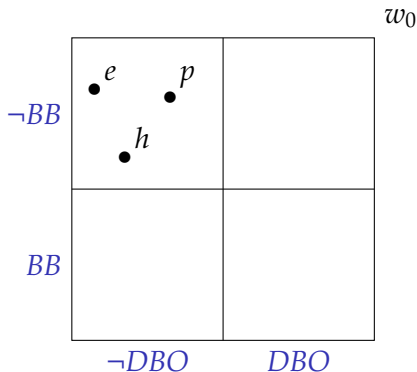
Dynamic Binding + Ordering Semantics



DBO = donkey that Balaam owns

BB = thing that Balaam beats

Dynamic Binding + Ordering Semantics



DBO = donkey that Balaam owns

BB = thing that Balaam beats

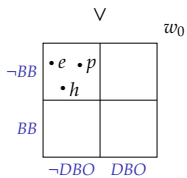
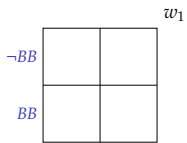
e = Eeyore

h = Herbert

p = Platero

w_0

$\neg BB$	$\bullet e \bullet p$ $\bullet h$	
BB		
	$\neg DBO$	DBO



		w_1
$\neg BB$	$\cdot e \cdot p$	
BB		$\cdot \mathbf{h}$

∨

		w_0
$\neg BB$	$\cdot e \cdot p$	
BB	$\cdot h$	
	$\neg DBO$	DBO

		w_2
$-BB$	$\cdot p$ $\cdot h$	$\cdot e$
BB		

∨

		w_1
$-BB$	$\cdot e$ $\cdot p$	
BB		$\cdot h$

∨

		w_0
$-BB$	$\cdot e$ $\cdot h$	$\cdot p$
BB		
	$\neg DBO$	DBO

$\neg BB$	$\cdot e$ $\cdot h$	$\cdot \mathbf{p}$	w_3
BB			

\vee

$\neg BB$	$\cdot p$ $\cdot h$	$\cdot \mathbf{e}$	w_2
BB			

\vee

$\neg BB$	$\cdot e \cdot p$		w_1
BB		$\cdot \mathbf{h}$	

\vee

$\neg BB$	$\cdot e \cdot p$ $\cdot h$		w_0
BB			

$\neg DBO$ DBO

$\neg BB$	$\cdot e$ $\cdot h$	$\cdot \mathbf{p}$	w_3
BB			

\vee

$\neg BB$	$\cdot p$ $\cdot h$	$\cdot \mathbf{e}$	w_2
BB			

\vee

$\neg BB$	$\cdot e$ $\cdot p$		w_1
BB		$\cdot \mathbf{h}$	

\vee

$\neg BB$	$\cdot e$ $\cdot p$ $\cdot h$		w_0
BB			

$\neg DBO$ DBO

$\langle w_0, g^{x \rightarrow h} \rangle$

$\langle w_0, g^{x \rightarrow e} \rangle$

$\langle w_0, g^{x \rightarrow p} \rangle$

$\neg BB$	$\cdot e$	$\cdot \mathbf{p}$	w_3
	$\cdot h$		
BB			

$\langle w_3, g^{x \rightarrow h} \rangle$

$\langle w_3, g^{x \rightarrow e} \rangle$

$\langle w_3, g^{x \rightarrow p} \rangle$

 \vee

$\neg BB$	$\cdot p$	$\cdot \mathbf{e}$	w_2
	$\cdot h$		
BB			

$\langle w_2, g^{x \rightarrow h} \rangle$

$\langle w_2, g^{x \rightarrow e} \rangle$

$\langle w_2, g^{x \rightarrow p} \rangle$

 \vee

$\neg BB$	$\cdot e$	$\cdot p$	w_1
BB		$\cdot \mathbf{h}$	

$\langle w_1, g^{x \rightarrow h} \rangle$

$\langle w_1, g^{x \rightarrow e} \rangle$

$\langle w_1, g^{x \rightarrow p} \rangle$

 \vee

$\neg BB$	$\cdot e$	$\cdot p$	w_0
	$\cdot h$		
BB			

$\langle w_0, g^{x \rightarrow h} \rangle$

$\langle w_0, g^{x \rightarrow e} \rangle$

$\langle w_0, g^{x \rightarrow p} \rangle$

 $\neg DBO \quad DBO$

$\neg BB$	$\cdot e$	$\cdot \mathbf{p}$	w_3
	$\cdot h$		
BB			

$$\langle w_3, g^{x \rightarrow h} \rangle = \langle w_3, g^{x \rightarrow e} \rangle = \langle w_3, g^{x \rightarrow p} \rangle$$

\vee

$\neg BB$	$\cdot p$	$\cdot \mathbf{e}$	w_2
	$\cdot h$		
BB			

$$\langle w_2, g^{x \rightarrow h} \rangle = \langle w_2, g^{x \rightarrow e} \rangle = \langle w_2, g^{x \rightarrow p} \rangle$$

\vee

$\neg BB$	$\cdot e \cdot p$		w_1
		$\cdot \mathbf{h}$	
BB			

$$\langle w_1, g^{x \rightarrow h} \rangle = \langle w_1, g^{x \rightarrow e} \rangle = \langle w_1, g^{x \rightarrow p} \rangle$$

\vee

$\neg BB$	$\cdot e \cdot p$		w_0
	$\cdot h$		
BB			

$$\langle w_0, g^{x \rightarrow h} \rangle = \langle w_0, g^{x \rightarrow e} \rangle = \langle w_0, g^{x \rightarrow p} \rangle$$

$\neg DBO$ DBO

$\neg BB$	$\cdot e$	$\cdot \mathbf{p}$	w_3
	$\cdot h$		
BB			

$$\langle w_3, g^{x \rightarrow h} \rangle = \langle w_3, g^{x \rightarrow e} \rangle = \langle w_3, g^{x \rightarrow p} \rangle$$

 \vee
 \vee

$\neg BB$	$\cdot p$	$\cdot \mathbf{e}$	w_2
	$\cdot h$		
BB			

$$\langle w_2, g^{x \rightarrow h} \rangle = \langle w_2, g^{x \rightarrow e} \rangle = \langle w_2, g^{x \rightarrow p} \rangle$$

 \vee
 \vee

$\neg BB$	$\cdot e \cdot p$		w_1
		$\cdot \mathbf{h}$	
BB			

$$\langle w_1, g^{x \rightarrow h} \rangle = \langle w_1, g^{x \rightarrow e} \rangle = \langle w_1, g^{x \rightarrow p} \rangle$$

 \vee
 \vee

$\neg BB$	$\cdot e \cdot p$		w_0
	$\cdot h$		
BB			

$$\langle w_0, g^{x \rightarrow h} \rangle = \langle w_0, g^{x \rightarrow e} \rangle = \langle w_0, g^{x \rightarrow p} \rangle$$

 $\neg DBO \quad DBO$

$\neg BB$	$\cdot e$	$\cdot \mathbf{p}$	w_3
	$\cdot h$		
BB			

$$\langle w_3, g^{x \rightarrow h} \rangle = \langle w_3, g^{x \rightarrow e} \rangle = \langle w_3, g^{x \rightarrow p} \rangle$$

\vee

\vee

$\neg BB$	$\cdot p$	$\cdot \mathbf{e}$	w_2
	$\cdot h$		
BB			

$$\langle w_2, g^{x \rightarrow h} \rangle = \langle w_2, g^{x \rightarrow e} \rangle = \langle w_2, g^{x \rightarrow p} \rangle$$

\vee

\vee

$\neg BB$	$\cdot e$	$\cdot p$	w_1
BB		$\cdot \mathbf{h}$	

$$\langle w_1, g^{x \rightarrow h} \rangle \neq \langle w_1, g^{x \rightarrow e} \rangle = \langle w_1, g^{x \rightarrow p} \rangle$$

\vee

\vee

$\neg BB$	$\cdot e$	$\cdot p$	w_0
	$\cdot h$		
BB			

$$\langle w_0, g^{x \rightarrow h} \rangle = \langle w_0, g^{x \rightarrow e} \rangle = \langle w_0, g^{x \rightarrow p} \rangle$$

$\neg DBO$ DBO

$\neg BB$	$\cdot e$	$\cdot \mathbf{p}$	w_3
	$\cdot h$		
BB			

$$\langle w_3, g^{x \rightarrow h} \rangle = \langle w_3, g^{x \rightarrow e} \rangle = \langle w_3, g^{x \rightarrow p} \rangle$$

 \vee
 \vee

$\neg BB$	$\cdot p$	$\cdot \mathbf{e}$	w_2
	$\cdot h$		
BB			

$$\langle w_2, g^{x \rightarrow h} \rangle \neq \langle w_2, g^{x \rightarrow e} \rangle \neq \langle w_2, g^{x \rightarrow p} \rangle$$

 \vee
 \vee

$\neg BB$	$\cdot e$	$\cdot p$	w_1
BB		$\cdot \mathbf{h}$	

$$\langle w_1, g^{x \rightarrow h} \rangle \neq \langle w_1, g^{x \rightarrow e} \rangle = \langle w_1, g^{x \rightarrow p} \rangle$$

 \vee
 \vee

$\neg BB$	$\cdot e$	$\cdot p$	w_0
	$\cdot h$		
BB			

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 $\neg DBO \quad DBO$

$\neg BB$	$\cdot e$	$\cdot \mathbf{p}$	w_3
	$\cdot h$		
BB			

$$\langle w_3, g^{x \rightarrow h} \rangle = \langle w_3, g^{x \rightarrow e} \rangle \neq \langle w_3, g^{x \rightarrow p} \rangle$$

 \vee
 \vee

$\neg BB$	$\cdot p$	$\cdot \mathbf{e}$	w_2
	$\cdot h$		
BB			

$$\langle w_2, g^{x \rightarrow h} \rangle \neq \langle w_2, g^{x \rightarrow e} \rangle \neq \langle w_2, g^{x \rightarrow p} \rangle$$

 \vee
 \vee

$\neg BB$	$\cdot e$	$\cdot p$	w_1
BB		$\cdot \mathbf{h}$	

$$\langle w_1, g^{x \rightarrow h} \rangle \neq \langle w_1, g^{x \rightarrow e} \rangle = \langle w_1, g^{x \rightarrow p} \rangle$$

 \vee
 \vee

$\neg BB$	$\cdot e$	$\cdot p$	w_0
	$\cdot h$		
BB			

$$\langle w_0, g^{x \rightarrow h} \rangle = \langle w_0, g^{x \rightarrow e} \rangle = \langle w_0, g^{x \rightarrow p} \rangle$$

 $\neg DBO \quad DBO$

$-BB$	$\cdot e$	$\cdot \mathbf{p}$	w_3
	$\cdot h$		
BB			

$$\langle w_3, g^{x \rightarrow h} \rangle = \langle w_3, g^{x \rightarrow e} \rangle \neq \langle w_3, g^{x \rightarrow p} \rangle$$

 \vee
 \vee

$-BB$	$\cdot p$	$\cdot \mathbf{e}$	w_2
	$\cdot h$		
BB			

$$\langle w_2, g^{x \rightarrow h} \rangle \neq \langle w_2, g^{x \rightarrow e} \rangle \neq \langle w_2, g^{x \rightarrow p} \rangle$$

 \vee
 \vee

$-BB$	$\cdot e$	$\cdot p$	w_1
BB		$\cdot \mathbf{h}$	

$$\langle w_1, g^{x \rightarrow h} \rangle \neq \langle w_1, g^{x \rightarrow e} \rangle = \langle w_1, g^{x \rightarrow p} \rangle$$

 \vee
 \vee

$-BB$	$\cdot e$	$\cdot p$	w_0
	$\cdot h$		
BB			

$$\langle w_0, g^{x \rightarrow h} \rangle = \langle w_0, g^{x \rightarrow e} \rangle = \langle w_0, g^{x \rightarrow p} \rangle$$

 $-DBO \quad DBO$

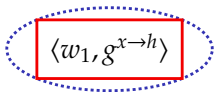
w_1

$-BB$	$\cdot e \cdot p$	
BB		$\cdot \mathbf{h}$
	$-DBO$	DBO

$$\langle w_1, g^{x \rightarrow h} \rangle$$

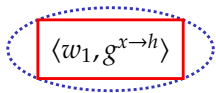
$$\exists x DBO(x) \square \rightarrow BB(x)$$

		w_1
$\neg BB$	$\cdot e \cdot p$	
BB		$\cdot \mathbf{h}$
	$\neg DBO$	DBO



$$\exists x DBO(x) \square \rightarrow BB(x)$$

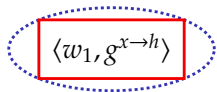
		w_1
$\neg BB$	$\cdot e \cdot p$	
BB		$\cdot \mathbf{h}$
	$\neg DBO$	DBO



$$\forall j (j \in f(A, i) \{j\} [BB(x)] \neq \emptyset)$$

$$\exists x DBO(x) \square \rightarrow BB(x)$$

		w_1
$\neg BB$	$\cdot e \cdot p$	
BB		$\cdot \mathbf{h}$
	$\neg DBO$	DBO

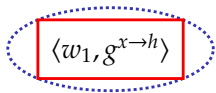


$$\forall j (j \in f(A, i) \{j\} [BB(x)] \neq \emptyset)$$

$$\{\langle w_1, g^{x \rightarrow h} \rangle\} [BB(x)]$$

$$\exists x DBO(x) \square \rightarrow BB(x)$$

		w_1
$\neg BB$	$\cdot e \cdot p$	
BB		$\cdot \mathbf{h}$
	$\neg DBO$	DBO



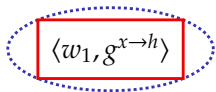
$$\forall j (j \in f(A, i) \{j\} [BB(x)] \neq \emptyset)$$

$$\{\langle w_1, g^{x \rightarrow h} \rangle\} [BB(x)]$$

$$w_1 \in \llbracket BB(h) \rrbracket?$$

$$\exists x DBO(x) \square \rightarrow BB(x)$$

		w_1
$\neg BB$	$\cdot e \cdot p$	
BB		$\cdot \mathbf{h}$
	$\neg DBO$	DBO



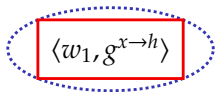
$$\forall j (j \in f(A, i) \{j\} [BB(x)] \neq \emptyset)$$

$$\{\langle w_1, g^{x \rightarrow h} \rangle\} [BB(x)]$$

$$w_1 \in \llbracket BB(h) \rrbracket? \checkmark$$

$$\exists x DBO(x) \square \rightarrow BB(x)$$

		w_1
$\neg BB$	$\cdot e \cdot p$	
BB		$\cdot \mathbf{h}$
	$\neg DBO$	DBO



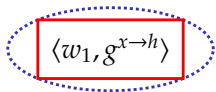
$$\forall j (j \in f(A, i) \{j\} [BB(x)] \neq \emptyset)$$

$$\{\langle w_1, g^{x \rightarrow h} \rangle\} [BB(x)] = \{\langle w_1, g^{x \rightarrow h} \rangle\} \neq \emptyset$$

$$w_1 \in \llbracket BB(h) \rrbracket? \checkmark$$

$$\exists x DBO(x) \sqcap \rightarrow BB(x) \checkmark$$

		w_1
$\neg BB$	$\cdot e \cdot p$	
BB		$\cdot \mathbf{h}$
	$\neg DBO$	DBO



$$\forall j (j \in f(A, i) \{j\} [BB(x)] \neq \emptyset)$$

$$\{\langle w_1, g^{x \rightarrow h} \rangle\} [BB(x)] = \{\langle w_1, g^{x \rightarrow h} \rangle\} \neq \emptyset$$

$$w_1 \in \llbracket BB(h) \rrbracket? \checkmark$$

Ordering Semantics + Dynamic Binding

Problem: no universal entailments

Ordering Semantics + Dynamic Binding

Problem: no universal entailments

- (11) If Balaam owned a donkey, he would beat it.
- (12)
 - a. If Herbert were a donkey Balaam owned, Balaam would beat Herbert.
 - b. If Eeyore were a donkey Balaam owned, Balaam would beat Eeyore.
 - c. If Platero were a donkey Balaam owned, Balaam would beat Platero.

Ordering Semantics + Dynamic Binding

Problem: no universal entailments

- (11) If Balaam owned a donkey, he would beat it.
- (12) a. If Herbert were a donkey Balaam owned, Balaam would beat Herbert.
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Ordering Semantics + Dynamic Binding

(12-b) If Eeyore were a donkey Balaam owned, Balaam would beat Eeyore.

(13) $DBO(e) \Box \rightarrow BB(e)$

$\neg BB$	$\cdot e$	$\cdot \mathbf{p}$	w_3
	$\cdot h$		
BB			

$$\langle w_3, g^{x \rightarrow h} \rangle = \langle w_3, g^{x \rightarrow e} \rangle = \langle w_3, g^{x \rightarrow p} \rangle$$

 \vee
 \vee

$\neg BB$	$\cdot p$	$\cdot \mathbf{e}$	w_2
	$\cdot h$		
BB			

$$\langle w_2, g^{x \rightarrow h} \rangle = \langle w_2, g^{x \rightarrow e} \rangle = \langle w_2, g^{x \rightarrow p} \rangle$$

 \vee
 \vee

$\neg BB$	$\cdot e \cdot p$		w_1
		$\cdot \mathbf{h}$	
BB			

$$\langle w_1, g^{x \rightarrow h} \rangle = \langle w_1, g^{x \rightarrow e} \rangle = \langle w_1, g^{x \rightarrow p} \rangle$$

 \vee
 \vee

$\neg BB$	$\cdot e \cdot p$		w_0
	$\cdot h$		
BB			

$$\langle w_0, g^{x \rightarrow h} \rangle = \langle w_0, g^{x \rightarrow e} \rangle = \langle w_0, g^{x \rightarrow p} \rangle$$

 $\neg DBO \quad DBO$

$\neg BB$	$\cdot e$	$\cdot \mathbf{p}$	w_3
	$\cdot h$		
BB			

$$\langle w_3, g^{x \rightarrow h} \rangle = \langle w_3, g^{x \rightarrow e} \rangle = \langle w_3, g^{x \rightarrow p} \rangle$$

 \vee
 \vee

$\neg BB$	$\cdot p$	$\cdot \mathbf{e}$	w_2
	$\cdot h$		
BB			

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 \vee
 \vee

$\neg BB$	$\cdot e \cdot p$		w_1
		$\cdot \mathbf{h}$	
BB			

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 \vee
 \vee

$\neg BB$	$\cdot e \cdot p$		w_0
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BB			

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 $\neg DBO \quad DBO$

$\neg BB$	$\cdot e$	$\cdot \mathbf{p}$	w_3
BB	$\cdot h$		

$$\langle w_3, g^{x \rightarrow h} \rangle = \langle w_3, g^{x \rightarrow e} \rangle = \langle w_3, g^{x \rightarrow p} \rangle$$

\vee

\vee

$\neg BB$	$\cdot p$	$\cdot \mathbf{e}$	w_2
BB	$\cdot h$		

$$\langle w_2, g^{x \rightarrow h} \rangle = \langle w_2, g^{x \rightarrow e} \rangle = \langle w_2, g^{x \rightarrow p} \rangle$$

\vee

\vee

$\neg BB$	$\cdot e \cdot p$		w_1
BB		$\cdot \mathbf{h}$	

$$\langle w_1, g^{x \rightarrow h} \rangle = \langle w_1, g^{x \rightarrow e} \rangle = \langle w_1, g^{x \rightarrow p} \rangle$$

\vee

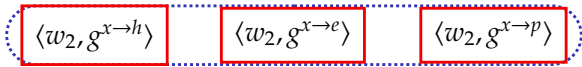
\vee

$\neg BB$	$\cdot e \cdot p$		w_0
BB	$\cdot h$		

$$\langle w_0, g^{x \rightarrow h} \rangle = \langle w_0, g^{x \rightarrow e} \rangle = \langle w_0, g^{x \rightarrow p} \rangle$$

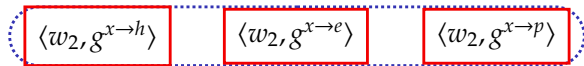
$\neg DBO$ DBO

		w_2
$-BB$	$\cdot p$ $\cdot h$	$\cdot e$
BB		
	$\neg DBO$	DBO



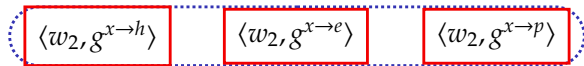
$DBO(e) \square \rightarrow BB(e)$

		w_2
$-BB$	$\cdot p$ $\cdot h$	$\cdot e$
BB		
	$\neg DBO$	DBO



		w_2
$-BB$	$\cdot p$ $\cdot h$	$\cdot e$
BB		
	$\neg DBO$	DBO

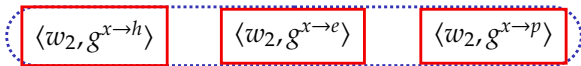
$DBO(e) \square \rightarrow BB(e)$



$$\forall j (j \in f(A, i)\{j\}[BB(e)] \neq \emptyset)$$

		w_2
$-BB$	$\cdot p$ $\cdot h$	$\cdot e$
BB		
	$\neg DBO$	DBO

$$DBO(e) \square \rightarrow BB(e)$$

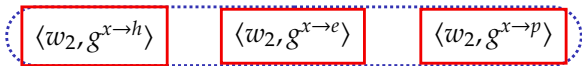


$$\forall j (j \in f(A, i)\{j\}[BB(e)] \neq \emptyset)$$

$$w_2 \in \llbracket BB(e) \rrbracket?$$

		w_2
$-BB$	$\cdot p$ $\cdot h$	$\cdot e$
BB		
	$\neg DBO$	DBO

$$DBO(e) \square \rightarrow BB(e)$$

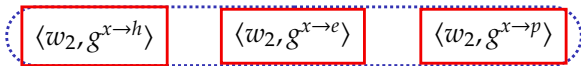


$$\forall j (j \in f(A, i) \{j\} [BB(e)] \neq \emptyset)$$

$$w_2 \in \llbracket BB(e) \rrbracket? \quad \times$$

		w_2
$-BB$	$\cdot p$ $\cdot h$	$\cdot e$
BB		
	$\neg DBO$	DBO

$DBO(e) \not\rightarrow BB(e)$ **X**



$\forall j (j \in f(A, i) \setminus \{j\} [BB(e)] \neq \emptyset$

$w_2 \in \llbracket BB(e) \rrbracket$? **X**

Ordering Semantics + Dynamic Binding

Problem: no universal entailments

- (14) If Balaam owned a donkey, he would beat it.
- (15)
 - a. If Herbert were a donkey Balaam owned, Balaam would beat Herbert.
 - b. **If Eeyore were a donkey Balaam owned, Balaam would beat Eeyore.**
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Ordering Semantics + Dynamic Binding

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How to fix this?

Ordering Semantics + Dynamic Binding

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How to fix this?

Route 1: special orderings

Route 2: high readings

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Walker and Romero (2015): universal entailments would follow from $A \sqsupset \rightarrow C$ iff the closeness ordering were such that

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for any $a, b \in \mathcal{D}$, the closest world which combines with $g^{x \rightarrow a}$ to form an A -possibility is as close as the closest world which combines with $g^{x \rightarrow b}$ to form an A -possibility.

Route 1: Special Orderings

Walker and Romero (2015): universal entailments would follow from $A \Box \rightarrow C$ iff the closeness ordering were such that

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An ordering set \mathcal{S} is *special* relative to a state s and sentence A

iff

$$(16) \quad \forall i(i \in s \supset \forall j(j \in /A/i \supset \exists k(k \in f(A, i) \wedge g_j = g_k)))$$

For all possibilities i in s , if j is an A -possibility for i , then among the nearest (relative to i) A -possibilities is a possibility which shares an assignment with j .

$\neg BB$	$\cdot e$ $\cdot h$	$\cdot \mathbf{p}$	w_3
BB			

\vee

$\neg BB$	$\cdot p$ $\cdot h$	$\cdot \mathbf{e}$	w_2
BB			

\vee

$\neg BB$	$\cdot e$ $\cdot p$		w_1
BB		$\cdot \mathbf{h}$	

\vee

$\neg BB$	$\cdot e$ $\cdot p$ $\cdot h$		w_0
BB			

$\neg DBO$ DBO

$\neg BB$	$\cdot e$ $\cdot h$	$\cdot \mathbf{p}$	w_3
BB			

\vee

$\neg BB$	$\cdot p$ $\cdot h$	$\cdot \mathbf{e}$	w_2
BB			

\vee

$\neg BB$	$\cdot e$ $\cdot p$		w_1
BB		$\cdot \mathbf{h}$	

\vee

$\neg BB$	$\cdot e$ $\cdot p$ $\cdot h$		w_0
BB			

$\neg DBO$ DBO

$\neg BB$	$\cdot e$ $\cdot h$	$\cdot \mathbf{p}$	w_3
BB			

\vee

$\neg BB$	$\cdot p$ $\cdot h$	$\cdot \mathbf{e}$	w_2
BB			

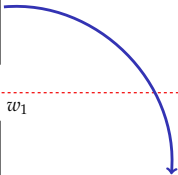
\vee

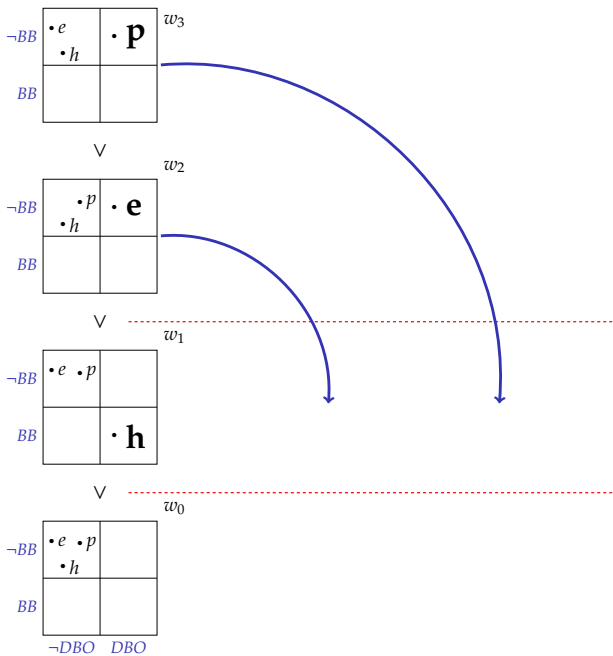
$\neg BB$	$\cdot e$ $\cdot p$		w_1
BB		$\cdot \mathbf{h}$	

\vee

$\neg BB$	$\cdot e$ $\cdot p$ $\cdot h$		w_0
BB			

$\neg DBO$ DBO





$\neg BB$	$\cdot e$	$\cdot \mathbf{p}$	w_3
BB	$\cdot h$		

||

$\neg BB$	$\cdot p$	$\cdot \mathbf{e}$	w_2
BB	$\cdot h$		

||

$\neg BB$	$\cdot e \cdot p$		w_1
BB		$\cdot \mathbf{h}$	

∨

$\neg BB$	$\cdot e \cdot p$		w_0
BB	$\cdot h$		

$\neg DBO$ DBO

$$\langle w_3, g^{x \rightarrow h} \rangle = \langle w_3, g^{x \rightarrow e} \rangle = \langle w_3, g^{x \rightarrow p} \rangle$$

||

$$\langle w_2, g^{x \rightarrow h} \rangle = \langle w_2, g^{x \rightarrow e} \rangle = \langle w_2, g^{x \rightarrow p} \rangle$$

||

$$\langle w_1, g^{x \rightarrow h} \rangle = \langle w_1, g^{x \rightarrow e} \rangle = \langle w_1, g^{x \rightarrow p} \rangle$$

∨

$$\langle w_0, g^{x \rightarrow h} \rangle = \langle w_0, g^{x \rightarrow e} \rangle = \langle w_0, g^{x \rightarrow p} \rangle$$

$-BB$	$\cdot e$	$\cdot \mathbf{p}$	w_3
BB	$\cdot h$		

||

$-BB$	$\cdot p$	$\cdot \mathbf{e}$	w_2
BB	$\cdot h$		

||

$-BB$	$\cdot e \cdot p$		w_1
BB		$\cdot \mathbf{h}$	

∨

$-BB$	$\cdot e \cdot p$		w_0
BB	$\cdot h$		

$-DBO$ DBO

$$\langle w_3, g^{x \rightarrow h} \rangle = \langle w_3, g^{x \rightarrow e} \rangle \neq \langle w_3, g^{x \rightarrow p} \rangle$$

||

$$\langle w_2, g^{x \rightarrow h} \rangle \neq \langle w_2, g^{x \rightarrow e} \rangle \neq \langle w_2, g^{x \rightarrow p} \rangle$$

||

$$\langle w_1, g^{x \rightarrow h} \rangle \neq \langle w_1, g^{x \rightarrow e} \rangle = \langle w_1, g^{x \rightarrow p} \rangle$$

∨

$$\langle w_0, g^{x \rightarrow h} \rangle = \langle w_0, g^{x \rightarrow e} \rangle = \langle w_0, g^{x \rightarrow p} \rangle$$

$-BB$	$\cdot e$	$\cdot \mathbf{p}$	w_3
BB	$\cdot h$		

||

$-BB$	$\cdot p$	$\cdot \mathbf{e}$	w_2
BB	$\cdot h$		

||

$-BB$	$\cdot e \cdot p$		w_1
BB		$\cdot \mathbf{h}$	

∨

$-BB$	$\cdot e \cdot p$		w_0
BB	$\cdot h$		

$-DBO$ DBO

$$\langle w_3, g^{x \rightarrow h} \rangle = \langle w_3, g^{x \rightarrow e} \rangle \neq \langle w_3, g^{x \rightarrow p} \rangle$$

||

$$\langle w_2, g^{x \rightarrow h} \rangle \neq \langle w_2, g^{x \rightarrow e} \rangle \neq \langle w_2, g^{x \rightarrow p} \rangle$$

||

$$\langle w_1, g^{x \rightarrow h} \rangle \neq \langle w_1, g^{x \rightarrow e} \rangle = \langle w_1, g^{x \rightarrow p} \rangle$$

∨

$$\langle w_0, g^{x \rightarrow h} \rangle = \langle w_0, g^{x \rightarrow e} \rangle = \langle w_0, g^{x \rightarrow p} \rangle$$

$-BB$	$\cdot e$ $\cdot h$	$\cdot p$	w_3
BB			

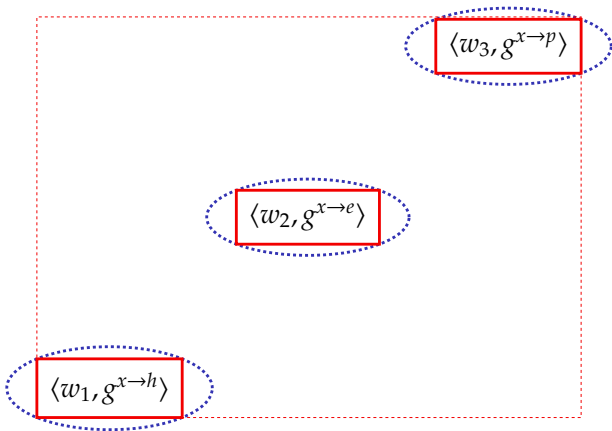
||

$-BB$	$\cdot p$ $\cdot h$	$\cdot e$	w_2
BB			

||

$-BB$	$\cdot e$ $\cdot p$		w_1
BB		$\cdot h$	

$-DBO$ DBO



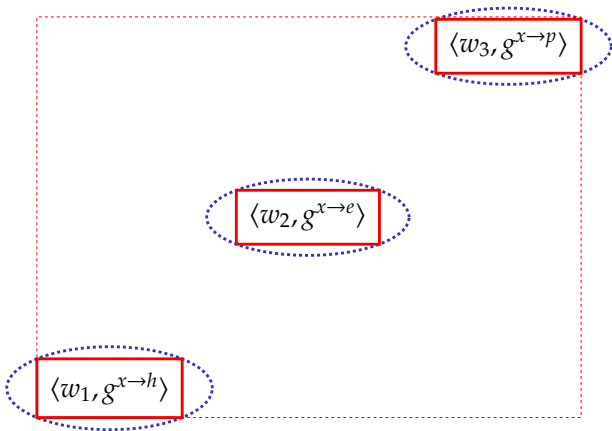
$-BB$	$\cdot e$	$\cdot \mathbf{p}$	w_3
	$\cdot h$		
BB			

||

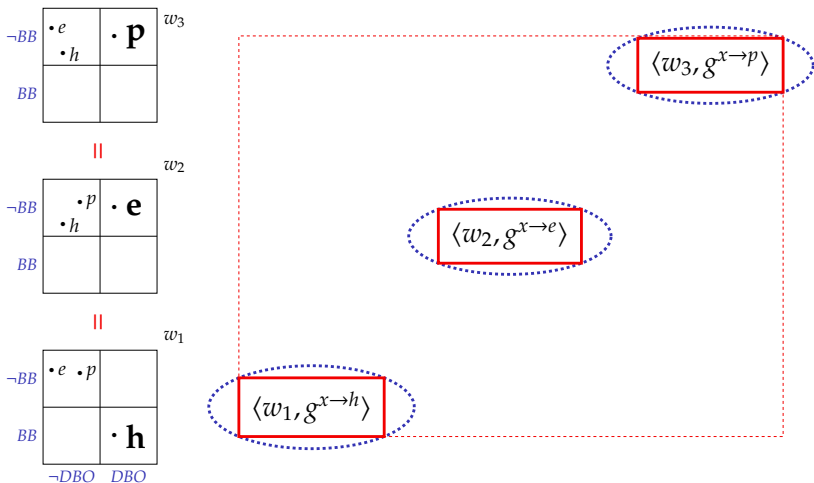
$-BB$	$\cdot p$	$\cdot \mathbf{e}$	w_2
	$\cdot h$		
BB			

||

$-BB$	$\cdot e$	$\cdot p$	w_1
BB		$\cdot \mathbf{h}$	
	$-DBO$	DBO	



$$\exists x DBO(x) \square \rightarrow BB(x)$$



$\exists x DBO(x) \square \rightarrow BB(x) \quad \times$

Route 2: High Readings

Leave world ordering \leq alone,

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Leave world ordering \leq alone, but define an assignment-sensitive similarity ordering \leq^* based on it.

$$(17) \quad j \leq_i^* k \text{ iff } w_j \leq_{w_i} w_k \wedge g_j = g_k$$

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Leave world ordering \leq alone, but define an assignment-sensitive similarity ordering \leq^* based on it.

$$(17) \quad j \leq_i^* k \text{ iff } w_j \leq_{w_i} w_k \wedge g_j = g_k$$

$$(18) \quad f^*(A, i) = \{j : j \in /A/i \wedge \neg \exists k(k \in /A/i \wedge k <_{w_i}^* j)\}.$$

$$(19) \quad s[A \Box \rightarrow C] = \{i : i \in s \wedge \forall j(j \in f^*(A, i) \supset \{j\}[C] \neq \emptyset)\}$$

$\neg BB$	$\cdot e$ $\cdot h$	$\cdot \mathbf{p}$	w_3
BB			

\vee

$\neg BB$	$\cdot p$ $\cdot h$	$\cdot \mathbf{e}$	w_2
BB			

\vee

$\neg BB$	$\cdot e \cdot p$		w_1
BB		$\cdot \mathbf{h}$	

\vee

$\neg BB$	$\cdot e \cdot p$ $\cdot h$		w_0
BB			

$\neg DBO$ DBO

$\neg BB$	$\cdot e$	$\cdot \mathbf{p}$	w_3
	$\cdot h$		
BB			

$\langle w_3, g^{x \rightarrow h} \rangle$

$\langle w_3, g^{x \rightarrow e} \rangle$

$\langle w_3, g^{x \rightarrow p} \rangle$

 \vee

$\neg BB$	$\cdot p$	$\cdot \mathbf{e}$	w_2
	$\cdot h$		
BB			

$\langle w_2, g^{x \rightarrow h} \rangle$

$\langle w_2, g^{x \rightarrow e} \rangle$

$\langle w_2, g^{x \rightarrow p} \rangle$

 \vee

$\neg BB$	$\cdot e$	$\cdot p$	w_1
BB		$\cdot \mathbf{h}$	

$\langle w_1, g^{x \rightarrow h} \rangle$

$\langle w_1, g^{x \rightarrow e} \rangle$

$\langle w_1, g^{x \rightarrow p} \rangle$

 \vee

$\neg BB$	$\cdot e$	$\cdot p$	w_0
	$\cdot h$		
BB			

$\langle w_0, g^{x \rightarrow h} \rangle$

$\langle w_0, g^{x \rightarrow e} \rangle$

$\langle w_0, g^{x \rightarrow p} \rangle$

 $\neg DBO \quad DBO$

$-BB$	$\cdot e$	$\cdot \mathbf{p}$	w_3
	$\cdot h$		
BB			

\vee

$-BB$	$\cdot p$	$\cdot \mathbf{e}$	w_2
	$\cdot h$		
BB			

\vee

$-BB$	$\cdot e$	$\cdot p$	w_1
BB		$\cdot \mathbf{h}$	

\vee

$-BB$	$\cdot e$	$\cdot p$	w_0
	$\cdot h$		
BB			

$\neg DBO$ DBO

$\langle w_3, g^{x \rightarrow h} \rangle$

$\langle w_3, g^{x \rightarrow e} \rangle$

$\langle w_3, g^{x \rightarrow p} \rangle$

$\langle w_2, g^{x \rightarrow h} \rangle$

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$\langle w_2, g^{x \rightarrow p} \rangle$

$\langle w_1, g^{x \rightarrow h} \rangle$

$\langle w_1, g^{x \rightarrow e} \rangle$

$\langle w_1, g^{x \rightarrow p} \rangle$

$\langle w_0, g^{x \rightarrow h} \rangle$

$\langle w_0, g^{x \rightarrow e} \rangle$

$\langle w_0, g^{x \rightarrow p} \rangle$

$-BB$	$\cdot e$	$\cdot \mathbf{p}$	w_3
BB	$\cdot h$		

\vee

$-BB$	$\cdot p$	$\cdot \mathbf{e}$	w_2
BB	$\cdot h$		

\vee

$-BB$	$\cdot e$	$\cdot p$	w_1
BB		$\cdot \mathbf{h}$	

\vee

$-BB$	$\cdot e$	$\cdot p$	w_0
BB	$\cdot h$		

$-DBO$ DBO

$$\langle w_3, g^{x \rightarrow h} \rangle$$

\neq

$$\langle w_3, g^{x \rightarrow e} \rangle$$

\neq

$$\langle w_3, g^{x \rightarrow p} \rangle$$

$$\langle w_2, g^{x \rightarrow h} \rangle$$

\neq

$$\langle w_2, g^{x \rightarrow e} \rangle$$

\neq

$$\langle w_2, g^{x \rightarrow p} \rangle$$

$$\langle w_1, g^{x \rightarrow h} \rangle$$

\neq

$$\langle w_1, g^{x \rightarrow e} \rangle$$

\neq

$$\langle w_1, g^{x \rightarrow p} \rangle$$

$$\langle w_0, g^{x \rightarrow h} \rangle$$

\neq

$$\langle w_0, g^{x \rightarrow e} \rangle$$

\neq

$$\langle w_0, g^{x \rightarrow p} \rangle$$

$-BB$	$\cdot e$	$\cdot \mathbf{p}$	w_3
BB	$\cdot h$		

 \vee

$-BB$	$\cdot p$	$\cdot \mathbf{e}$	w_2
BB	$\cdot h$		

 \vee

$-BB$	$\cdot e \cdot p$		w_1
BB		$\cdot \mathbf{h}$	

 \vee

$-BB$	$\cdot e \cdot p$		w_0
BB	$\cdot h$		

 $-DBO \quad DBO$
 $\langle w_3, g^{x \rightarrow h} \rangle$
 \neq
 $\langle w_3, g^{x \rightarrow e} \rangle$
 \neq
 $\langle w_3, g^{x \rightarrow p} \rangle$
 \checkmark
 \checkmark
 \checkmark
 $\langle w_2, g^{x \rightarrow h} \rangle$
 \neq
 $\langle w_2, g^{x \rightarrow e} \rangle$
 \neq
 $\langle w_2, g^{x \rightarrow p} \rangle$
 \checkmark
 \checkmark
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 $\langle w_1, g^{x \rightarrow h} \rangle$
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 \neq
 $\langle w_1, g^{x \rightarrow p} \rangle$
 \checkmark
 \checkmark
 \checkmark
 $\langle w_0, g^{x \rightarrow h} \rangle$
 \neq
 $\langle w_0, g^{x \rightarrow e} \rangle$
 \neq
 $\langle w_0, g^{x \rightarrow p} \rangle$

$-BB$	$\cdot e$	$\cdot \mathbf{p}$	w_3
	$\cdot h$		
BB			

 \vee

$-BB$	$\cdot p$	$\cdot \mathbf{e}$	w_2
	$\cdot h$		
BB			

 \vee

$-BB$	$\cdot e$	$\cdot p$	w_1
BB		$\cdot \mathbf{h}$	

 \vee

$-BB$	$\cdot e$	$\cdot p$	w_0
	$\cdot h$		
BB			

 $-DBO$ DBO

$$\langle w_3, g^{x \rightarrow h} \rangle$$

 \neq

$$\langle w_3, g^{x \rightarrow e} \rangle$$

 \neq

$$\langle w_3, g^{x \rightarrow p} \rangle$$

 \checkmark
 \checkmark
 \checkmark

$$\langle w_2, g^{x \rightarrow h} \rangle$$

 \neq

$$\langle w_2, g^{x \rightarrow e} \rangle$$

 \neq

$$\langle w_2, g^{x \rightarrow p} \rangle$$

 \checkmark
 \checkmark
 \checkmark

$$\langle w_1, g^{x \rightarrow h} \rangle$$

 \neq

$$\langle w_1, g^{x \rightarrow e} \rangle$$

 \neq

$$\langle w_1, g^{x \rightarrow p} \rangle$$

 \checkmark
 \checkmark
 \checkmark

$$\langle w_0, g^{x \rightarrow h} \rangle$$

 \neq

$$\langle w_0, g^{x \rightarrow e} \rangle$$

 \neq

$$\langle w_0, g^{x \rightarrow p} \rangle$$

$-BB$	$\cdot e$	$\cdot \mathbf{p}$	w_3
	$\cdot h$		
BB			

 \vee

$-BB$	$\cdot p$	$\cdot \mathbf{e}$	w_2
	$\cdot h$		
BB			

 \vee

$-BB$	$\cdot e \cdot p$		w_1
		$\cdot \mathbf{h}$	
BB			

 \vee

$-BB$	$\cdot e \cdot p$		w_0
	$\cdot h$		
BB			

 $-DBO$ DBO

$$\langle w_3, g^{x \rightarrow h} \rangle$$

 \neq

$$\langle w_3, g^{x \rightarrow e} \rangle$$

 \neq

$$\langle w_3, g^{x \rightarrow p} \rangle$$

 \checkmark
 \checkmark
 \checkmark

$$\langle w_2, g^{x \rightarrow h} \rangle$$

 \neq

$$\langle w_2, g^{x \rightarrow e} \rangle$$

 \neq

$$\langle w_2, g^{x \rightarrow p} \rangle$$

 \checkmark
 \checkmark
 \checkmark

$$\langle w_1, g^{x \rightarrow h} \rangle$$

 \neq

$$\langle w_1, g^{x \rightarrow e} \rangle$$

 \neq

$$\langle w_1, g^{x \rightarrow p} \rangle$$

 \checkmark
 \checkmark
 \checkmark

$$\langle w_0, g^{x \rightarrow h} \rangle$$

 \neq

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$-BB$	$\cdot e$	$\cdot p$	w_3
	$\cdot h$		
BB			

 \vee

$-BB$	$\cdot p$	$\cdot e$	w_2
	$\cdot h$		
BB			

 \vee

$-BB$	$\cdot e$	$\cdot p$	w_1
BB		$\cdot h$	

 \vee

$-BB$	$\cdot e$	$\cdot p$	w_0
	$\cdot h$		
BB			

 $-DBO$ DBO

$$\langle w_3, g^{x \rightarrow h} \rangle$$

 \neq

$$\langle w_3, g^{x \rightarrow e} \rangle$$

 \neq

$$\langle w_3, g^{x \rightarrow p} \rangle$$

 \checkmark

$$\langle w_2, g^{x \rightarrow h} \rangle$$

 \neq

$$\langle w_2, g^{x \rightarrow e} \rangle$$

 \neq

$$\langle w_2, g^{x \rightarrow p} \rangle$$

 \checkmark

$$\langle w_1, g^{x \rightarrow h} \rangle$$

 \neq

$$\langle w_1, g^{x \rightarrow e} \rangle$$

 \neq

$$\langle w_1, g^{x \rightarrow p} \rangle$$

 \checkmark

$$\langle w_0, g^{x \rightarrow h} \rangle$$

 \neq

$$\langle w_0, g^{x \rightarrow e} \rangle$$

 \neq

$$\langle w_0, g^{x \rightarrow p} \rangle$$

$\neg BB$	$\cdot e$	$\cdot p$	w_3
	$\cdot h$		
BB			

 \vee

$\neg BB$	$\cdot p$	$\cdot e$	w_2
	$\cdot h$		
BB			

 \vee

$\neg BB$	$\cdot e$	$\cdot p$	w_1
BB		$\cdot h$	

 \vee

$\neg BB$	$\cdot e$	$\cdot p$	w_0
	$\cdot h$		
BB			

 $\neg DBO$ DBO
 $\langle w_3, g^{x \rightarrow h} \rangle$
 \neq
 $\langle w_3, g^{x \rightarrow e} \rangle$
 \neq
 $\langle w_3, g^{x \rightarrow p} \rangle$
 \checkmark
 \checkmark
 \checkmark
 $\langle w_2, g^{x \rightarrow h} \rangle$
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 $\langle w_1, g^{x \rightarrow h} \rangle$
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 $\langle w_1, g^{x \rightarrow p} \rangle$
 \checkmark
 \checkmark
 \checkmark
 $\langle w_0, g^{x \rightarrow h} \rangle$
 \neq
 $\langle w_0, g^{x \rightarrow e} \rangle$
 \neq
 $\langle w_0, g^{x \rightarrow p} \rangle$

$-BB$	$\cdot e$	$\cdot \mathbf{p}$	w_3
BB	$\cdot h$		

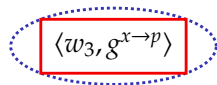
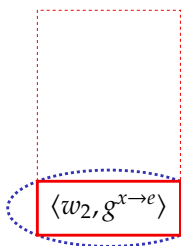
\vee

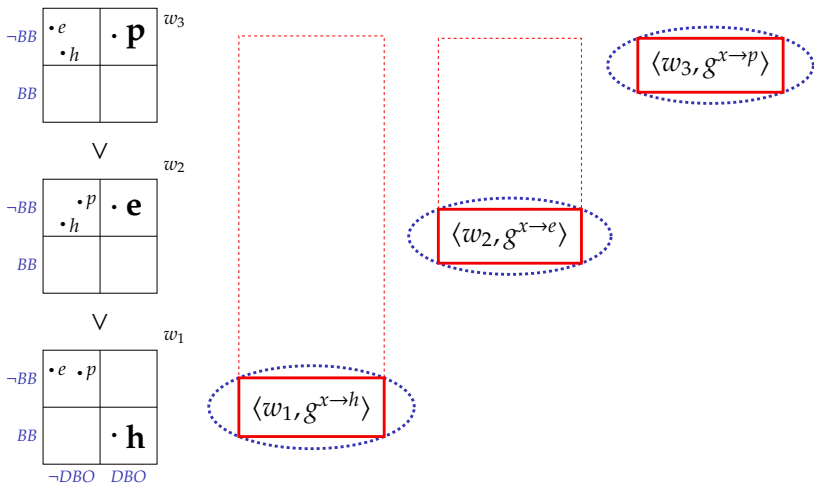
$-BB$	$\cdot p$	$\cdot \mathbf{e}$	w_2
BB	$\cdot h$		

\vee

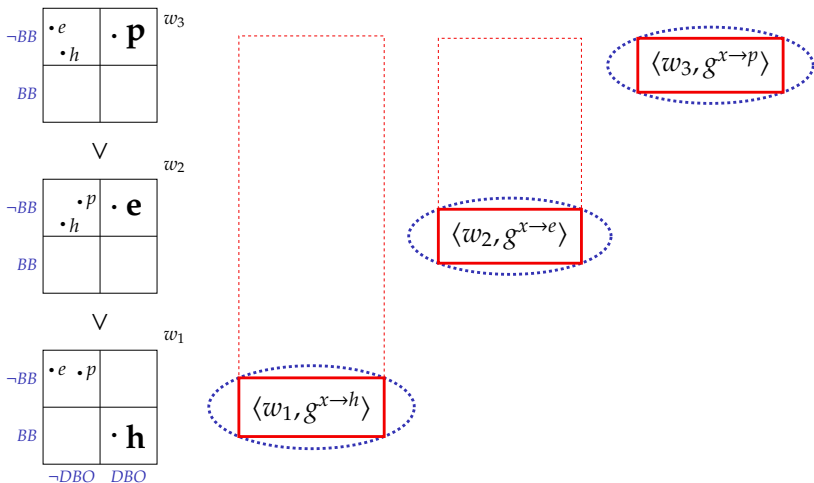
$-BB$	$\cdot e$	$\cdot p$	w_1
BB		$\cdot \mathbf{h}$	

$\neg DBO$ DBO

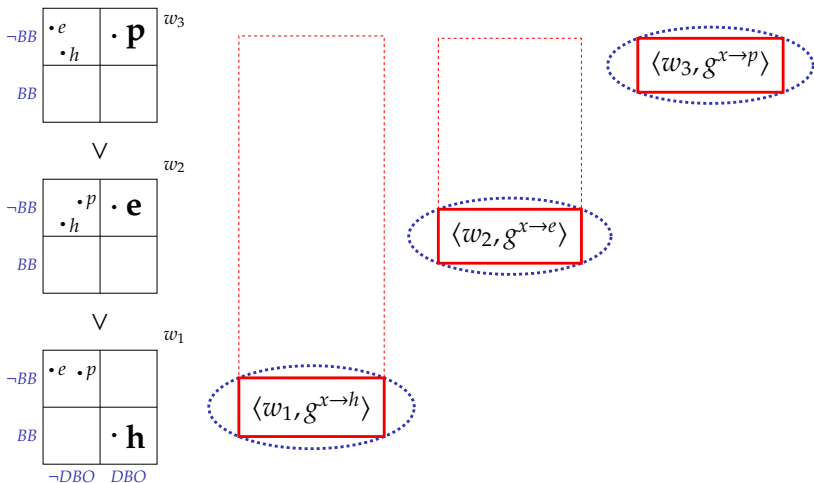




$$\exists x DBO(x) \square \rightarrow BB(x)$$



$$\exists x DBO(x) \square \rightarrow BB(x)$$



$\exists x DBO(x) \square \rightarrow BB(x)$ ✗

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Problem for Special Orderings?

Takeaway

New Data - Summary

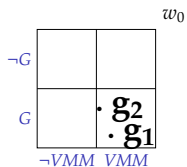
- (1) *Allie*: If Mary had made a vase, she would have made it from glass.
- (2) *Bert*: But she could have made a clay vase (and she wouldn't have made *that* from glass)!

Case 1: Mary made two glass vases.

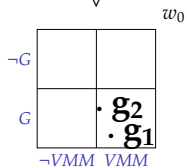
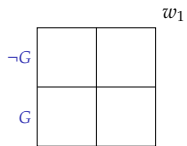
Case 2: Mary did not make any vases.

	Case 1	Case 2
(1)	✓	✗
(2)	??	✓

Problem for High Readings



Problem for High Readings



Problem for High Readings

		w_1
$-G$	$\cdot g_2$	$\cdot \mathbf{c}$
G		$\cdot \mathbf{g}_1$

v

		w_0
$-G$		
G	$\cdot \mathbf{g}_2$	$\cdot \mathbf{g}_1$

$-VMM \quad VMM$

Problem for High Readings

		w_1
$-G$	$\cdot g_2$	$\cdot c$
G		$\cdot g_1$

V

		w_0
$-G$		
G	$\cdot g_2$	$\cdot g_1$
	$-VMM$	VMM

$$\langle w_0, g^{x \rightarrow g_1} \rangle$$

$$\langle w_0, g^{x \rightarrow g_2} \rangle$$

$$\langle w_0, g^{x \rightarrow c} \rangle$$

Problem for High Readings

		w_1
$-G$	$\cdot g_2$	$\cdot c$
G		$\cdot g_1$

\vee

		w_0
$-G$		
G		$\cdot g_2$ $\cdot g_1$

\neg VMM VMM

$$\langle w_1, g^{x \rightarrow g_1} \rangle$$

$$\langle w_1, g^{x \rightarrow g_2} \rangle$$

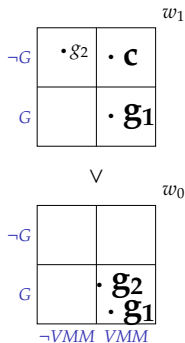
$$\langle w_1, g^{x \rightarrow c} \rangle$$

$$\langle w_0, g^{x \rightarrow g_1} \rangle$$

$$\langle w_0, g^{x \rightarrow g_2} \rangle$$

$$\langle w_0, g^{x \rightarrow c} \rangle$$

Problem for High Readings



$$\langle w_1, g^{x \rightarrow g_1} \rangle \neq \langle w_1, g^{x \rightarrow g_2} \rangle \neq \langle w_1, g^{x \rightarrow c} \rangle$$
$$\langle w_0, g^{x \rightarrow g_1} \rangle \neq \langle w_0, g^{x \rightarrow g_2} \rangle \neq \langle w_0, g^{x \rightarrow c} \rangle$$

Problem for High Readings

		w_1
$-G$	$\cdot g_2$	$\cdot c$
G		$\cdot g_1$
	\vee	
		w_0
$-G$		
G		$\cdot g_2$
		$\cdot g_1$
	$-VMM$	VMM

$\langle w_1, g^{x \rightarrow g_1} \rangle$	\neq	$\langle w_1, g^{x \rightarrow g_2} \rangle$	\neq	$\langle w_1, g^{x \rightarrow c} \rangle$
$\cdot \vee$		$\cdot \vee$		$\cdot \vee$
$\langle w_0, g^{x \rightarrow g_1} \rangle$	\neq	$\langle w_0, g^{x \rightarrow g_2} \rangle$	\neq	$\langle w_0, g^{x \rightarrow c} \rangle$

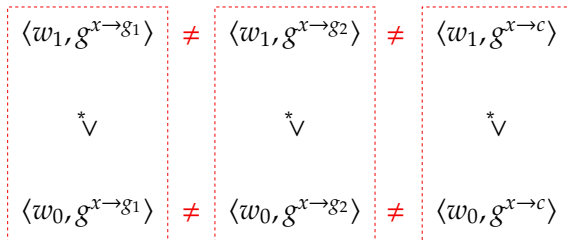
Problem for High Readings

		w_1
$\neg G$	• g_2 • c	
G	• g_1	
	\vee	

		w_0
$\neg G$		
G	• g_2 • g_1	
	\vee	

$\neg VMM$ VMM

$\exists x VMM(x) \square \rightarrow G(x)$



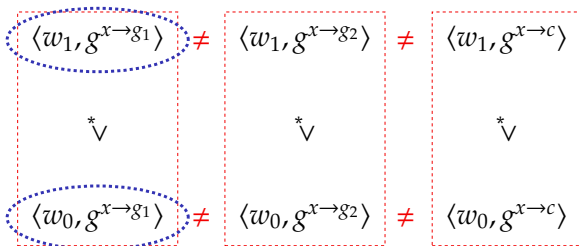
Problem for High Readings

		w_1
$\neg G$	• g_2	• c
G		• g_1
	\vee	

		w_0
$\neg G$		
G	• g_2	• g_1
	\vee	

$\neg VMM$ VMM

$\exists x VMM(x) \square \rightarrow G(x)$



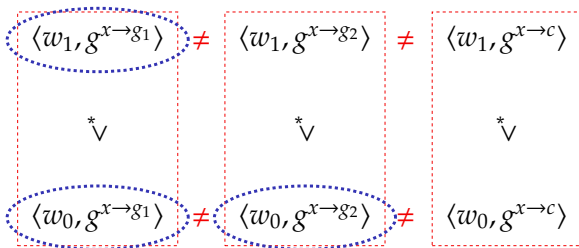
Problem for High Readings

		w_1
-G	• g_2	• c
G		• g_1
	\vee	

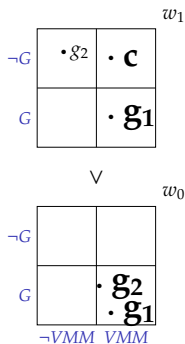
		w_0
-G		
G	• g_2	• g_1
	\vee	

$\neg VMM$ VMM

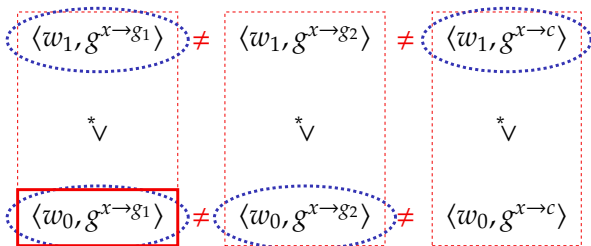
$\exists x VMM(x) \square \rightarrow G(x)$



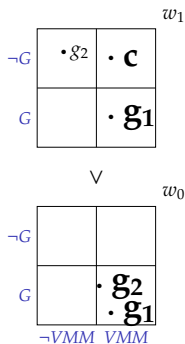
Problem for High Readings



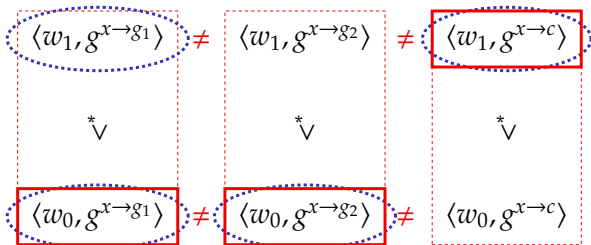
$\exists x VMM(x) \square \rightarrow G(x)$



Problem for High Readings



$\exists x VMM(x) \square \rightarrow G(x)$

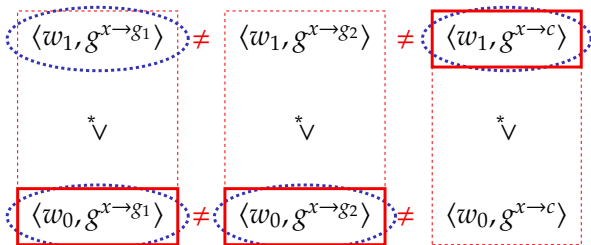


Problem for High Readings

		w_1
-G	• g_2 • c	
G	• g₁	
	∨	
		w_0
-G		
G	• g₂ • g₁	
	∨	
	-VMM VMM	

$\exists x VMM(x) \square \rightarrow G(x)$

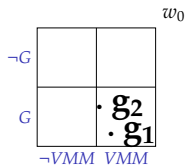
$w_1 \in \llbracket G(c) \rrbracket?$



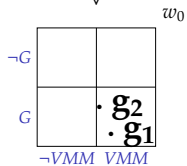
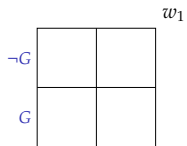
Success of Special Orderings

Assumption: \leq is *strongly centered*: $w_0 <_{w_0} w_1$

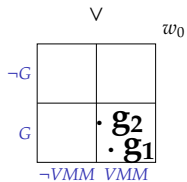
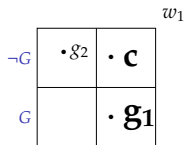
Success of Special Orderings



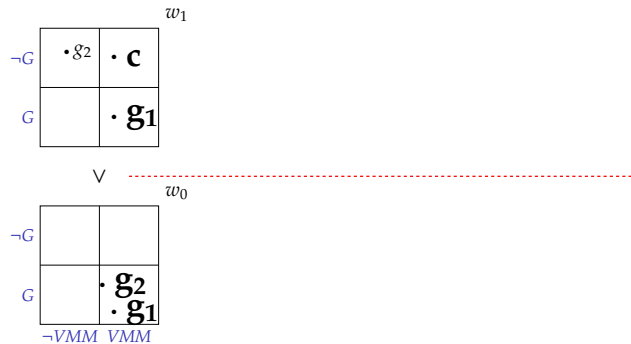
Success of Special Orderings



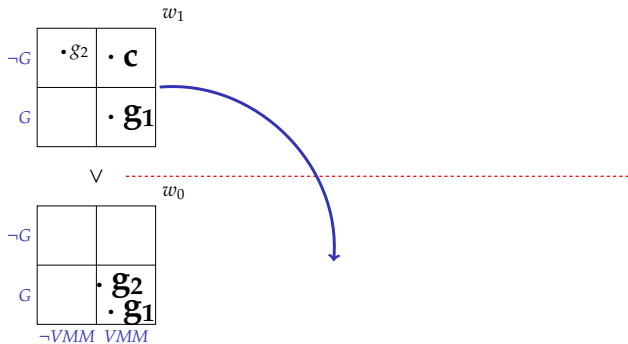
Success of Special Orderings



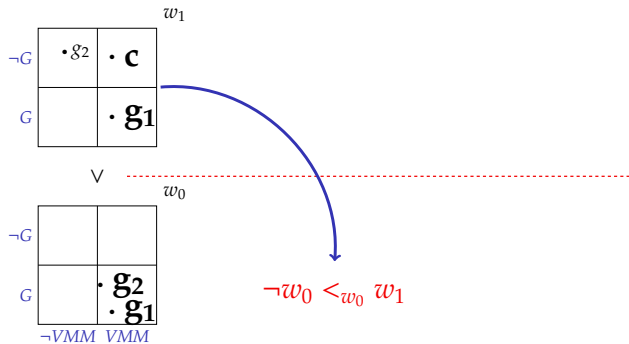
Success of Special Orderings



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Right predictions about the new data.

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Saving High Readings: Weak?

Objection: the high reading accounts have ways of dealing with weak/low readings as well.

- (20) a. If I had a dime, I would put it in the meter.
- b. If I had picked a number, I would have picked 3.

Saving High Readings: Weak?

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No. Consider

Case 3: Mary made one glass vase and one clay vase.

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- b. If I had picked a number, I would have picked 3.

This vase case is just one of those.

No. Consider

Case 3: Mary made one glass vase and one clay vase.

(1) false in this case, which is not what we'd expect on a weak/low reading.

Saving High Readings: QDR?

c in Case 1 gets ignored due to quantifier domain restriction.

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Maybe, but how can this get Case 2 right?

Saving High Readings: QDR?

c in Case 1 gets ignored due to quantifier domain restriction.

Maybe, but how can this get Case 2 right? Shouldn't the possible clay vase be irrelevant still?

Problem for Special Orderings?

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Walker and Romero (2015): cases of universal entailments without special order.

Problem for Special Orderings?

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- (21) SCENARIO: Balaam took part in a game show which had the following format. If you win the easy first round, you win Herbert, an obnoxious and disobedient donkey. The reward for the much more difficult second and third rounds are the well-mannered and obedient donkeys Eeyore and Platero, respectively. Losing a round of the game eliminates the player, keeping them from advancing to any later rounds. Balaam was eliminated in the first round, and so remains donkeyless.

Problem for Special Orderings?

John, only aware of the game's first round, asserts (22), since he knows about Balaam's short temper.

(22) If Balaam owned a donkey, he would beat it.

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(23) No, Balaam could have won Platero or Eeyore too, and he wouldn't beat either of them if he owned them.

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(23) No, Balaam could have won Platero or Eeyore too, and he wouldn't beat either of them if he owned them.

Seems like Sarah is right, so there are universal entailments. But intuitively, the world where Balaam wins only one round is more similar to the actual world than ones where he wins two or three. So no special order.

Problem for Special Orderings?

Response part 1:

Problem for Special Orderings?

Response part 1: closeness ordering need not correspond to intuitive ordering.

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Recall Fine (1975):

- (24) a. If Nixon pressed the button, there would have been a nuclear holocaust. ✓
- b. If Nixon had pressed the button, the wire would have miraculously malfunctioned. ✗

Problem for Special Orderings?

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Disaster for ordering semantics?

Problem for Special Orderings?

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Disaster for ordering semantics?

Lewis (1979): weight violations of law more than disparities in other facts.

We still need a theory of the closeness ordering that predicts special orderings in the right cases, but nothing has ruled this out yet.

Problem for Special Orderings?

Response part 2: actually, the high reading account needs special orderings too.

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- (25) SCENARIO: Cory, who is donkeyless, is a bit crazy. He's disposed to take out his anger on his most prized possession. He also took part in the game show described in (21), but also lost in the first round. Had he won any rounds, the prize from the most advanced round he won would have become his prized possession, and he would have beaten it, but he wouldn't beat anything else.

Now consider the following.

- (26) If Cory owned a donkey, he would beat it.

Problem for Special Orderings?

Response part 2: actually, the high reading account needs special orderings too.

- (25) SCENARIO: Cory, who is donkeyless, is a bit crazy. He's disposed to take out his anger on his most prized possession. He also took part in the game show described in (21), but also lost in the first round. Had he won any rounds, the prize from the most advanced round he won would have become his prized possession, and he would have beaten it, but he wouldn't beat anything else.

Now consider the following.

- (26) If Cory owned a donkey, he would beat it.

In this scenario, the salient reading of (26) seems false. If Cory had owned Eeyore, he would own but not beat Herbert.

Problem for Special Orderings?

To get this right, the high reading account needs the worlds where Cory wins 2 or 3 donkeys to be as close as the one where he wins 1. It needs a special ordering.

But then we can get the right results from the special ordering alone, without the high reading.

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Takeaway

Counterfactual donkey sentences have universal entailments, but not of the sort we'd expect from high reading accounts.

The special ordering account seems to get things right. But we still need a theory of how these orderings arise.

Thanks!

References

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